

# NAG Fortran Library Routine Document

## F06VKF

**Note:** before using this routine, please read the Users' Note for your implementation to check the interpretation of *bold italicised* terms and other implementation-dependent details.

### 1 Purpose

F06VKF performs one of the permutation operations

$$\begin{aligned} B &\leftarrow P^T B, & B &\leftarrow PB, \\ B &\leftarrow BP^T \quad \text{or} & B &\leftarrow BP, \end{aligned}$$

where  $B$  is a complex matrix, and  $P$  is a permutation matrix.

$P$  is represented in the form

$$P = P_{1,p_1} P_{2,p_2} \cdots P_{n,p_n},$$

where  $P_{i,j}$  is the permutation matrix that interchanges items  $i$  and  $j$ ; that is,  $P_{i,j}$  is the unit matrix with rows and columns  $i$  and  $j$  interchanged. If  $i = j$ ,  $P_{i,j} = I$ .

Let  $m$  denote the number of rows of  $B$  if  $\text{SIDE} = \text{'L'}$ , or the number of columns of  $B$  if  $\text{SIDE} = \text{'R'}$ : the routine does not require  $m$  to be passed as an argument, but assumes that  $m \geq p_i$  for  $i = 1, \dots, n$ .

This routine requires the indices  $p_i$  to be supplied in an *double precision* array (the routine takes the integer part of the array elements); F06VJF performs the same operation with the indices supplied in an INTEGER array.

### 2 Specification

```
SUBROUTINE F06VKF (SIDE, TRANS, N, PERM, K, B, LDB)
  INTEGER          N, K, LDB
  double precision PERM(*)
  complex*16     B(LDB,*)
  CHARACTER*1     SIDE, TRANS
```

### 3 Description

None.

### 4 References

None.

### 5 Parameters

1:	SIDE – CHARACTER*1	<i>Input</i>
2:	TRANS – CHARACTER*1	<i>Input</i>

*On entry:* specify the operation to be performed as follows:

if  $\text{SIDE} = \text{'L'}$  and  $\text{TRANS} = \text{'T'}$ ,  $B \leftarrow P^T B$ ;  
 if  $\text{SIDE} = \text{'L'}$  and  $\text{TRANS} = \text{'N'}$ ,  $B \leftarrow PB$ ;  
 if  $\text{SIDE} = \text{'R'}$  and  $\text{TRANS} = \text{'T'}$ ,  $B \leftarrow BP^T$ ;  
 if  $\text{SIDE} = \text{'R'}$  and  $\text{TRANS} = \text{'N'}$ ,  $B \leftarrow BP$ .

*Constraint:*  $\text{SIDE} = \text{'L'}$  or  $\text{'R'}$ ;  $\text{TRANS} = \text{'N'}$  or  $\text{'T'}$ .

- 3: N – INTEGER *Input*  
*On entry:*  $n$ , the number of interchanges in the representation of  $P$ .  
*Constraint:*  $N \geq 0$ .
- 4: PERM(\*) – *double precision* array *Input*  
*On entry:* the  $n$  indices  $p_i$  which define the interchanges in the representation of  $P$ . It is usual to have  $p_i \geq i$ , but this is not necessary.  
*Constraint:*  $1 \leq \text{PERM}(i) \leq m$ .
- 5: K – INTEGER *Input*  
*On entry:*  $k$ , the number of columns of  $B$  if SIDE = 'L', or the number of rows of  $B$  if SIDE = 'R'.  
*Constraint:*  $K \geq 0$ .
- 6: B(LDB,\*) – *complex\*16* array *Input/Output*  
**Note:** the second dimension of the array B must be at least  $\max(1, K)$  if SIDE = 'L' and at least  $\max(1, m)$  if SIDE = 'R'.  
*On entry:* the original matrix  $B$ ;  $B$  is  $m$  by  $k$  if SIDE = 'L', or  $k$  by  $m$  if SIDE = 'R'.  
*On exit:* the permuted matrix  $B$ .
- 7: LDB – INTEGER *Input*  
*On entry:* the first dimension of the array B as declared in the (sub)program from which F06VKF is called.  
*Constraint:*  $LDB \geq \max(1, m)$  if SIDE = 'L';  $LDB \geq \max(1, K)$  if SIDE = 'R'.

## 6 Error Indicators and Warnings

None.

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